

Modulated electronic configurations in selectively doped multilayered nanostructures

V. M. Loktev¹, Yu. G. Pogorelov²

¹*N.N. Bogolyubov Institute for Theoretical Physics, Metrologichna 14b, Kiev 03134, Ukraine,*

²*IFIMUP, Universidade do Porto, R. Campo Alegre, 687, Porto 4169-007*

A simple theoretical model is proposed to describe the recent experimental results on formation of induced superconducting state and anomalous tunneling characteristics in selectively doped multilayered nanostructures based on La_2CuO_4 perovskite. In particular, it is shown that the structure composed from the nominally non-superconducting (undoped and overdoped) layers turns to be superconducting with superconductivity confined to narrow regions near the interfaces, in agreement with the experimental observations.

PACS numbers: 73.40.Gk, 73.50.-h, 73.61.-r

Recent experiments by Bozovic *et al* [1] provided a new intriguing insight on electronic properties of nanostructured perovskite systems. Using thorough epitaxy techniques available in Brookhaven National Laboratory [2–4], they were able to selectively introduce a well controlled level (including zero) of Sr dopants into each particular La_2CuO_4 layer (along the c -axis) and then observed unusual electronic characteristics of the composite structures. For instance, a stack of 15 alternating $(\text{La}_{2-x}\text{Sr}_x\text{CuO}_4)_4(\text{La}_2\text{CuO}_4)_2$ blocks with $x = 0.45$, that is alternating overdoped [5] and undoped (both separately non-superconducting) layers, revealed superconductivity with the critical temperature $T_c = 30$ K [1]. The authors interpreted this behavior as an evidence for carriers delocalization beyond the nominally doped region of the multilayered system. Below we propose a very simple theoretical model permitting a qualitative and semi-quantitative explanation of such delocalization effect.

The heuristic basis for the model is the assumption that the collective electronic states in the multilayered system are superpositions of almost uncoupled (because of a very slow c -axis hopping t_c) planar states in each j th La_2CuO_4 layer, formed by the fast ab -hopping $t_{ab} \gg t_c$ in the energy band of width $W = 8t_{ab}$ around the relevant atomic level and shifted by a certain local electric potential φ_j . The latter is related to the local charge densities $\rho_j = e(p_j - x_j)$ by mobile holes with density p_j and ionized dopants with density x_j (where e is the elementary charge), accordingly to the discrete version of the common Poisson equation:

$$\varphi_{j+1} + \varphi_{j-1} - 2\varphi_j = -\frac{4\pi c}{\varepsilon_{\text{eff}} a^2} \rho_j, \quad (1)$$

where a and c are the in-plane and c -axis lattice parameters and ε_{eff} is the (static) dielectric constant that effectively reduces the Coulomb field in the c -direction. This equation would be exact for potentials in a stack of mathematical planes, with uniform charge densities ρ_j and separation c , and should model real $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ layers where p_j delocalized holes and x_j localized dopants are distributed in different atomic planes within the period c of j th layer. The adopted form of purely dielectric

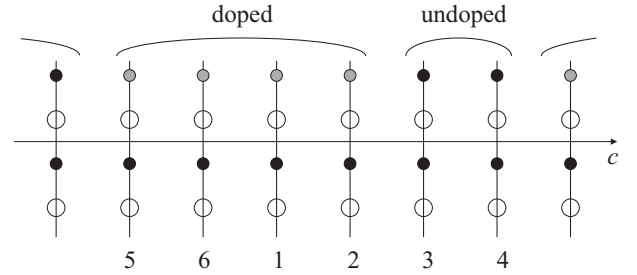


FIG. 1: Schematic of nanostructured system with periodically introduced dopants (light grey circles) into consecutive layers of La_2CuO_4 along the c -axis. There are only 3 independent values of electronic density over 6 layers in a period.

screening is justified in neglect of c -hopping processes, accordingly to their above mentioned weakness. We note that the charge densities ρ_j naturally vanish both in uniformly doped ($p_j = x_j$) and undoped ($p_j = x_j = 0$) systems.

Otherwise, the hole carrier density p_j is defined by the respective density of states (DOS) $g_j(\varepsilon)$:

$$p_j = 2 \int_{\varepsilon_F}^{W/2 - e\varphi_j} g_j(\varepsilon) d\varepsilon, \quad (2)$$

including the spin factor 2. Thus the role of c -hopping in this model is reduced to establishing the common Fermi level ε_F for all the layers. Using the simplest approximation of rectangular DOS: $g_j(\varepsilon) = 1/W$ within the bandwidth W , we arrive at the linear relation between p_j and φ_j :

$$e\varphi_j = \frac{1 - p_j}{2} W - \varepsilon_F. \quad (3)$$

Then inserting Eq. 3 into Eq. 1 leads to a non-uniform linear system for the densities p_j :

$$p_{j+1} + p_{j-1} - (2 + \alpha)p_j = -\alpha x_j, \quad (4)$$

where the dimensionless value:

$$\alpha = \frac{8\pi c e^2}{W \varepsilon_{\text{eff}} a^2} \quad (5)$$

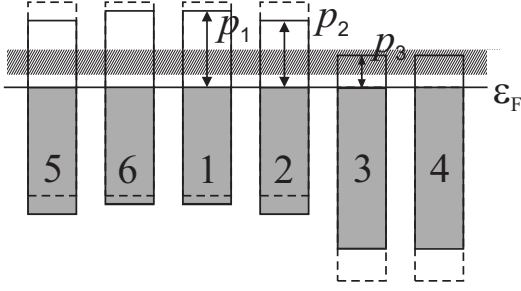


FIG. 2: Modulated electronic configuration by the shifted energy bands (solid rectangles) in the nanostructured system by Fig. 1, calculated for $x = 0.45$ and localization parameter $\alpha = 1$. The dashed rectangles indicate unshifted energy bands for isolated doped and undoped layers, and the hatched stripe marks the interval of carrier densities where superconductivity should exist.

is a single material parameter of the model, describing the localization degree of charge density fluctuations in the nanostructured system (less delocalization for bigger α). The advantage of Eq. 4 against an analogous system for potentials φ_j is in eliminating the Fermi level (doping dependent) and, notably, this system assures the total electroneutrality condition $\sum_i \rho_j = 0$. The present approach can be seen as a more detailed alternative to the phenomenological Thomas-Fermi treatment [6].

It is elementary to resolve Eq. 4 for the densities through the doping levels: $p_j = \sum_{j'} f_{jj'}(\alpha) x_{j'}$. The problem is reasonably simplified considering it periodic, then the period of n layers at given α fully defines the coefficients $f_{jj'}(\alpha)$ for $1 \leq j, j' \leq n$. For the sake of definiteness, let us consider the sample system like that in the experiment, Ref. [1], with $n = 6$ and $x_1 = x_2 = x_5 = x_6 \equiv x$, $x_3 = x_4 = 0$ (Fig. 1). The explicit solution of Eq. 4 in this case reads:

$$\begin{aligned} p_1 &= p_6 = \left(1 - \frac{1}{(\alpha+1)(\alpha+3)}\right)x, \\ p_2 &= p_5 = \frac{\alpha+2}{\alpha+3}x, \\ p_3 &= p_4 = \frac{\alpha+2}{(\alpha+1)(\alpha+3)}x, \end{aligned} \quad (6)$$

satisfying the evident electroneutrality condition $p_1 + p_2 + p_3 = 2x$.

Using the soft X-ray resonant scattering techniques [4] for direct measurement of carrier densities in the experiment, Ref. [6], yielded: $p_1^{\text{exp}} \approx 0.33$, $p_2^{\text{exp}} \approx 0.24$, $p_3^{\text{exp}} \approx 0.15$. A reasonable fit to this set can be achieved from Eq. 6 with the choice of $\alpha = 1$: $p_1^{\text{theor}} \approx 0.315$, $p_2^{\text{theor}} \approx 0.27$, $p_3^{\text{theor}} \approx 0.135$, that is within the experimental error of ± 0.03 from the measured values.

In order to relate these carrier densities with the experimentally defined critical temperatures, we can employ the phenomenological bell-like dependence:

$$T_{\text{ph}}(p) = (p_{\text{max}} - p)(p - p_{\text{min}})T^*, \quad (7)$$

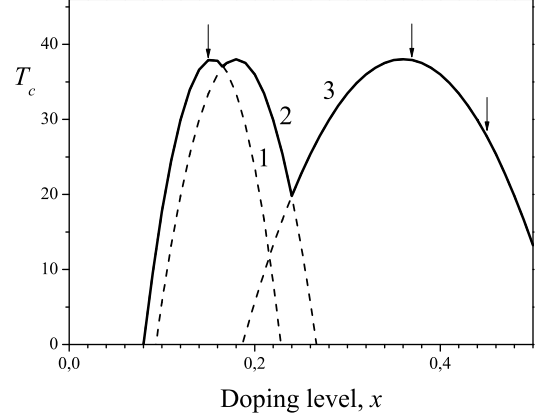


FIG. 3: Calculated critical temperature T_c vs doping level x for the $(\text{La}_{2-x}\text{Sr}_x\text{CuO}_4)_4 (\text{La}_2\text{CuO}_4)_2$ system. Three numbered curves refer to the respective layers from Fig. 2 and arrows indicate the doping levels of 0.15, 0.36 and 0.45 as in the experimental systems [1, 6].

with $p_{\text{min}} = 0.07$, $p_{\text{max}} = 0.2$, and $T^* = 9000$ K (this curve being slightly below of the commonly reported $T_c(p)$ in bulk LSCO [5]). Using $p = p_3^{\text{theor}}$ in Eq. 7 yields the value of $T_c \approx 38$ K, just that observed in Ref. [6]. This confirms the conclusion that the SC state in this system is limited to the nominally undoped layers 3,4 as represented schematically in Fig. 2.

One can compare the fitted value of $\alpha = 1$ with the theoretical expression, Eq. 5, using the standard values $a \approx 0.38$ nm, $c = 1.3$ nm and $W \approx 2$ eV. This suggests as high value of ε_{eff} as ~ 150 , however it does not seem unrealistic if the static c -axis polarizability for La_2CuO_4 [7, 8] is enhanced by a contribution from doped mobile carriers.

The situation can be further traced at varying the doping level x (with α supposedly constant). Thus, for $x = 0.45$ we obtain respectively: $p_1^{\text{theor}} \approx 0.395$, $p_2^{\text{theor}} \approx 0.34$, $p_3^{\text{theor}} \approx 0.165$, and then using this p_3^{theor} in Eq. 7 results in $T_c \approx 30$ K, again in agreement with the measured value [1].

At least, for the nominally optimum doping level $x = 0.15$, we have: $p_1 = 0.132$, $p_2 = 0.113$ and $p_3 = 0.055$, and the SC state with almost maximum T_c should persist only in the doped 1,2,5,6 layers separated by the insulating 3,4 layers. This agrees with the observation of blocked tunneling through the undoped La_2CuO_4 layer sandwiched between optimally doped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ electrodes [1].

Furthermore, combining the results, Eq. 6, and the phenomenological dependence, Eq. 7, one can easily build a model dependence for critical temperature of SC transition in the given $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4 - \text{La}_2\text{CuO}_4$ system vs the doping level x . As seen from Fig. 3, this dependence chosen as the maximum value from three bell-like curves: $T_c(p) = \max_j T_{\text{ph}}(p_j(x))$, has generally a

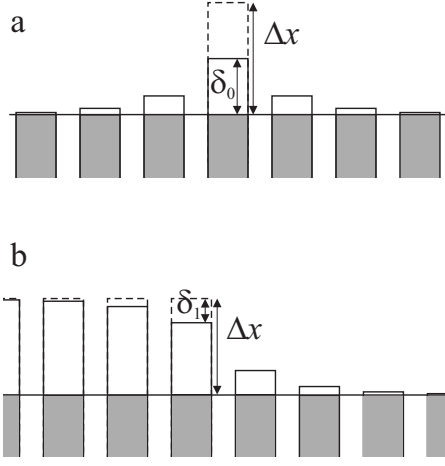


FIG. 4: Modulated electronic configurations for a) single doped layer between undoped semispaces and b) interface between two semispaces with different doping levels.

non-monotonous behavior with the broadest region contributed by the 3,4 layers. It should be noted that the SC state realized in this region may be of special interest since much longer lifetimes of charge carriers in the nominally undoped layers, in similarity with the well explored physics of 2D electron gas (2DEG) inverse layers in semiconducting heterojunctions [9]. This can be an important property for envisaged superconducting devices in nanotailored heterosystems [10] or excitonic superconductors [11].

The model, Eqs. 1-5 can be easily extended to other characteristic nanostructures. Thus, inclusion into an infinite stack of layers with some uniform doping level x of a single layer with different level $x + \Delta x$ will produce a symmetric distribution of carrier densities $p_j = p_{-j}$ that obviously tend to the asymptotic value: $p_{j \rightarrow \infty} \rightarrow x$. Then, considering the reduced densities $\delta_j = p_j - x$, we obtain from Eq. 4 an infinite set of linear equations:

$$\begin{aligned} (2 + \alpha)\delta_0 - 2\delta_1 &= \alpha\Delta x, \\ (2 + \alpha)\delta_j &= \delta_{j+1} + \delta_{j-1}, \quad j \geq 1, \end{aligned} \quad (8)$$

with the electroneutrality condition $\delta_0 + 2 \sum_{j \geq 1} \delta_j = \Delta x$. It can be easily checked that the system, Eq. 8, is solved

with $\delta_j = \delta_0 \exp(-\kappa j)$ where $\kappa = \text{arccosh}(1 + \alpha/2)$ and with the most interesting central value given by $\delta_0 = \Delta x \tanh \kappa/2 = \Delta x \sqrt{\alpha/(a+4)}$. From this function, it follows that the greatest part of added charge density remains at the central layer, $\delta_0 > \Delta x/2$, when the localization parameter α surpasses 4/3. Though being somewhat higher of that used in the previous analysis of periodically doped system, such value can be supposed to describe a stronger localization for the single layer doping. Then it can support the experimental observation of persisting SC state in a single optimally doped layer sandwiched between undoped semispaces ($x = 0$, $\Delta x = x_{\text{opt}}$) [12], if p_0 falls within the range $[p_{\text{min}}, p_{\text{max}}]$. Contrary-wise, a single undoped layer ($x_0 = 0$) between optimally doped semispaces ($x = x_{\text{opt}} = -\Delta x$) should possess a lower local density $p_0 = x_{\text{opt}} - \delta_0$, which more probably goes out of $[p_{\text{min}}, p_{\text{max}}]$ so that this layer would pertain insulating.

Another exemplary case is the interface between two semi-infinite stacks of layers with different uniform doping levels $x_j = x$ at $j \leq -1$ and $x_j = x - \Delta x$ at $j \geq 1$, where the reduced densities can be defined respectively as $\delta_j = x_1 - p_j$ at $j \leq -1$ and $\delta_j = p_j - x_2$ at $j \geq 1$ with evident symmetry $\delta_j = \delta_{-j}$. Then Eq. 8 is reformulated as:

$$\begin{aligned} (3 + \alpha)\delta_1 - \delta_2 &= \Delta x = x_1 - x_2, \\ (2 + \alpha)\delta_j &= \delta_{j+1} + \delta_{j-1}, \quad j \geq 2, \end{aligned} \quad (9)$$

and its solution is given by $\delta_j = \delta_1 \exp[-\kappa(j - 1)]$ with the same κ as above and with $\delta_1 = \Delta x / [2 - \alpha/2 + \sqrt{\alpha(\alpha + 4)}]$.

At least, combining the previous cases can serve to explain the "giant proximity effect" observed in a thick underdoped layer sandwiched between optimally doped electrodes [13].

In conclusion, a simple electrostatic model combined with 2D electronic band spectrum is used to semi-quantitatively explain the recent experimental findings in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ multilayered systems, selectively doped with precision to single atomic layer. Exact solutions are found for local charge densities p in conducting CuO_2 planes, for a number of periodic and non-periodic doping configurations, permitting agreement with the experimentally defined p 's and SC transition critical temperature T_c . The model can be used for effective designing of new SC (including Josephson tunnel) systems.

[1] I. Bozovic, Phys. Usp. **51**, 170 (2008).
[2] I. Bozovic, J.N. Eckstein, G.F. Virshup, Physica C **235-240**, 178 (1994).
[3] I. Bozovic, IEEE Trans. Appl. Superconduct. **11**, 2686 (2001).
[4] A. Gozar, G. Logvenov, V.Y. Budko, I. Bozovic, Phys. Rev. B **75**, R201402 (2007).

[5] M.A. Kastner, R.J. Birgeneau, G. Shirane, Y. Endoh, Rev. Mod. Phys. **70**, 897 (1998).
[6] S. Smadici, J.C.T. Lee, S. Wang, P. Abbamonte, A. Gozar, G. Logvenov, C.D. Cavellin, I. Bozovic, arXiv: 0805.3189 (2008).
[7] C.Y. Chen, N.W. Preyer, P.J. Picone, M.A. Kastner, H.P. Jenssen, D.R. Gabbe, A. Cassanho, R.J. Birgeneau,

- Phys. Rev. Lett. **63**, 2307 (1989).
- [8] D. Reagor, E. Ahrens, S-W. Cheong, A. Migliori, Z. Fisk, Phys. Rev. Lett. **62**, 2048 (1989).
 - [9] C. Weisbuch, B. Vinter, *Quantum Semiconductor Structures: Fundamentals and Applications*, Academic Press, London, 1991.
 - [10] C. B. Eom, R. J. Cava, J. M. Phillips, D. J. Werder, J. Appl. Phys. **77**, 5449 (1995).
 - [11] V.L. Ginzburg, Phys. Lett. **13**, 101 (1964).
 - [12] I. Bozovic, G. Logvenov, M.A.J. Verhoeven, P. Caputo, E. Goldobin, T.H. Geballe, Nature **422**, 873 (2003).
 - [13] I. Bozovic, G. Logvenov, M.A.J. Verhoeven, P. Caputo, E. Goldobin, M.R. Beasley, Phys. Rev. Lett **93**, 157002 (2004).